

B-tree-Insert (T, K)

1. $r \leftarrow \text{root}[T]$
2. if $n[r] = 2t - 1$
3. then $S \leftarrow \text{allocate-node}()$
4. $\text{root}[T] \leftarrow S$
5. $\text{leaf}[S] \leftarrow \text{False}$
6. $n[S] \leftarrow 0$
7. $c_1[S] \leftarrow r$
8. $\text{B-tree-split-child}(S, 1, r)$
9. $\text{B-tree-Insert-Nonfull}(S, K)$
10. else $\text{B-tree-Insert-Nonfull}(r, K)$

B-tree-Insert-NonFull (x, K)

1. $i \leftarrow n[x]$
2. if $\text{leaf}[x]$
3. then while $i \geq 1$ and $K < \text{key}_i[x]$
4. do $\text{key}_{i+1}[x] \leftarrow \text{key}_i[x]$
5. $i \leftarrow i - 1$
6. $\text{key}_{i+1}[x] \leftarrow K$

The median key $key_t[y]$ is moved up to y 's parent.

- To reduce # of disk operations, whenever we travel down the tree searching for the position to insert, we split each full node we visit along the way.

B-tree-Split-child (x, i, y) // $C_i[x] = y$ is full

1. $z \leftarrow \text{allocate-node}()$
2. $\text{leaf}[z] \leftarrow \text{leaf}[y]$
3. $n[z] \leftarrow t-1$
4. for $j \leftarrow 1$ to $t-1$
5. do $\text{key}_j[z] \leftarrow \text{key}_{j+t}[y]$
6. if not leaf $[y]$
7. then for $j \leftarrow 1$ to t
8. do $C_j[z] \leftarrow C_{j+t}[y]$

set up the new n

9. $n[y] \leftarrow t-1$

10. for $j \leftarrow n[x]+1$ down to $i+1$

11. do $C_{j+1}[x] \leftarrow C_j[x]$

12. $C_{i+1}[x] \leftarrow z$

13. for $j \leftarrow n[x]$ down to i

14. do $\text{key}_{j+1}[x] \leftarrow \text{key}_j[x]$

15. $\text{key}_i[x] \leftarrow \text{key}_t[y]$

16. $n[x] \leftarrow n[x]+1$

17. Disk-Write (y)

18. Disk-Write (z)

19. Disk-Write (x)

update the
parent node x
after move up
 $\text{key}_t[y]$

$\Theta(t)$ running time

$O(1)$ disk operations.

Fig 18.5 illustrate this operation.

8. B-tree-Split-Child (s, l, r)
9. B-tree-Insert-Nonfull (s, k)
10. else B-tree-Insert-Nonfull (r, k)

B-tree-Insert-NonFull (x, k)

1. $i \leftarrow n[x]$
2. if leaf [x]
3. then while $i \geq 1$ and $k < \text{key}_i[x]$
4. do $\text{key}_{i+1}[x] \leftarrow \text{key}_i[x]$
5. $i \leftarrow i - 1$
6. $\text{key}_{i+1}[x] \leftarrow k$
7. $n[x] \leftarrow n[x] + 1$
8. Disk-Write (x)
9. else while $i \geq 1$ and $k < \text{key}_i[x]$
10. do $i \leftarrow i - 1$
11. $i \leftarrow i + 1$
12. Disk-Read ($c_i[x]$)
13. if $n[c_i[x]] \geq t - 1$
14. then B-tree-Split-Child ($x, i,$
15. if $k > \text{key}_i[x]$
16. then $i \leftarrow i + 1$
17. B-tree-Insert-Nonfull ($c_i[x], k$)

Fig 18.7 on page 448 shows various cases of ins